

# School District of Marshfield Course Syllabus

Course Name: Pre-Algebra Length of Course: 1 Year Credit: 1

# **Program Goal:**

The School District of Marshfield Mathematics Program will prepare students for college and career in the 21<sup>st</sup> century by ensuring *all* students learn based on skills and knowledge needed to succeed in post-secondary education/training, career, and life. The 4K through High School Mathematics curriculum is designed to support every student in achieving success. Students will be placed in to the driver's seat. Innovative educators will tailor instruction to student need through engaging learning activities and relevant assessment.

#### **Course Description:**

The class is self-paced using a computer program called Accelerated Math from Renaissance Learning. A student must master all objectives to successfully pass the course. Students will develop skills in Number Sense and Operation, Relationships with Quantities, Reasoning with Equations, Algebra Concepts, Linear and Exponential Relationships, Geometry and Measurement, Congruence, Proof and Construction, Connecting Algebra and Geometry through Coordinates, Data Analysis, Statistics and Probability.

**NOTE**: A calculator is required for this course. **PREREQUISITES**: Instructor's recommendation.

| Standards:   |   |  |  |  |
|--|---|--|--|--|
| Wisconsin Standards for Mathematical Practice (MP)   |   |  |  |  |
| MP: 1, 2, 3, 4, 5, 6, 7, 8   | <ol> <li>Make sense of problems and persevere in solving them.</li> <li>Reason abstractly and quantitatively.</li> <li>Construct viable arguments and critique the reasoning<br/>of others.</li> <li>Model with mathematics.</li> <li>Use appropriate tools strategically.</li> <li>Attend to precision.</li> <li>Look for and make use of structure.</li> <li>Look for and express regularity in repeated reasoning.</li> </ol>  |  |  |  |
| Wisconsin Standards for Mathematic   |   |  |  |  |
|  | s- Number and Quantity  |  |  |  |
| <b>The Real Number System (N-RN)</b><br><b>Use properties of rational and</b><br><b>irrational numbers.</b><br>N-RN: 3 | 3. Explain why the sum or product of two rational<br>numbers is rational; that the sum of a rational number and<br>an irrational number is irrational; and that the product of a<br>nonzero rational number and an irrational number is<br>irrational.  |  |  |  |
| Quantities (N-Q)   | indional.   |  |  |  |
| <b>Reason quantitatively and use units to solve problems.</b><br>N-Q: 1  | 1. Use units as a way to understand problems and to guide<br>the solution of multi-step problems; choose and interpret<br>units consistently in formulas; choose and interpret the<br>scale and the origin in graphs and data displays.   |  |  |  |
| Wisconsin Standards for Mathematic   | s- Algebra  |  |  |  |
| Seeing Structure in Expressions (A-SSE)  |   |  |  |  |
| <b>Interpret the structure of expressions.</b><br>A-SSE: 1a  | <ol> <li>Interpret expressions that represent a quantity in terms<br/>of its context.         <ol> <li>Interpret parts of an expression, such as terms,<br/>factors, and coefficients.</li> </ol> </li> </ol>   |  |  |  |
| Arithmetic with Polynomials and Ration   |   |  |  |  |
| Perform arithmetic operations on<br>polynomials.<br>A-APR: 1   | 1. Understand that polynomials form a system analogous<br>to the integers, namely, they are closed under the<br>operations of addition, subtraction, and multiplication;<br>add, subtract, and multiply polynomials.  |  |  |  |
| Creating Equations (A-CED)   |   |  |  |  |
| <b>Create equations that describe</b><br><b>numbers or relationships.</b><br>A-CED: 1, 2, 4                            | <ol> <li>Create equations and inequalities in one variable and<br/>use them to solve problems. <i>Include equations arising</i><br/><i>from linear and quadratic functions, and simple rational</i><br/><i>and exponential functions.</i></li> <li>Create equations in two or more variables to represent<br/>relationships between quantities; graph equations on<br/>coordinate axes with labels and scales.</li> <li>Rearrange formulas to highlight a quantity of interest,<br/>using the same reasoning as in solving equations. For<br/>example, rearrange Ohm's law V = IR to highlight</li> </ol> |  |  |  |

| <b>Reasoning with Equations and Inequalit</b>  | Reasoning with Equations and Inequalities (A-REI)                   |  |  |  |  |
|--|---|--|--|--|--|
| Understand solving equations as a              | 1. Explain each step in solving a simple equation as                |  |  |  |  |
| process of reasoning and explain the           | following from the equality of numbers asserted at the              |  |  |  |  |
| reasoning.                                     | previous step, starting from the assumption that the                |  |  |  |  |
| A-REI: 1                                       | original equation has a solution. Construct a viable                |  |  |  |  |
|  | argument to justify a solution method.                              |  |  |  |  |
| Solve equations and inequalities in one        | 3. Solve linear equations and inequalities in one variable,         |  |  |  |  |
| variable.                                      | including equations with coefficients represented by                |  |  |  |  |
| A-REI: 3                                       | letters.  |  |  |  |  |
| Wisconsin Standards for Mathematics- Functions |   |  |  |  |  |
| <b>Interpreting Functions (F-IF)</b>           |   |  |  |  |  |
| Understand the concept of a function           | 1. Understand that a function from one set (called the              |  |  |  |  |
| and use function notation.                     | domain) to another set (called the range) assigns to each           |  |  |  |  |
| F-IF: 1, 2                                     | element of the domain exactly one element of the range. If          |  |  |  |  |
|  | f is a function and x is an element of its domain, then $f(x)$      |  |  |  |  |
|  | denotes the output of $f$ corresponding to the input $x$ . The      |  |  |  |  |
|  | graph of <i>f</i> is the graph of the equation $y = f(x)$ .         |  |  |  |  |
|  | 2. Use function notation, evaluate functions for inputs in          |  |  |  |  |
|  | their domains, and interpret statements that use function           |  |  |  |  |
|  | notation in terms of a context.                                     |  |  |  |  |
| Interpret functions that arise in              | 4. For a function that models a relationship between two            |  |  |  |  |
| applications in terms of the context.          | quantities, interpret key features of graphs and tables in          |  |  |  |  |
| F-IF: 4, 5, 6                                  | terms of the quantities, and sketch graphs showing key              |  |  |  |  |
|  | features given a verbal description of the relationship. <i>Key</i> |  |  |  |  |
|  | features include: intercepts; intervals where the function          |  |  |  |  |
|  | is increasing, decreasing, positive, or negative; relative          |  |  |  |  |
|  | maximums and minimums; symmetries; end behavior; and                |  |  |  |  |
|  | periodicity.  |  |  |  |  |
|  | 5. Relate the domain of a function to its graph and, where          |  |  |  |  |
|  | applicable, to the quantitative relationship it describes.          |  |  |  |  |
|  | For example, if the function $h(n)$ gives the number of             |  |  |  |  |
|  | person-hours it takes to assemble n engines in a factory,           |  |  |  |  |
|  | then the positive integers would be an appropriate domain           |  |  |  |  |
|  | for the function.   |  |  |  |  |
|  | 6. Calculate and interpret the average rate of change of a          |  |  |  |  |
|  | function (presented symbolically or as a table) over a              |  |  |  |  |
|  | specified interval. Estimate the rate of change from a              |  |  |  |  |
|  | graph.  |  |  |  |  |
| Analyze functions using different              | 7. Graph functions expressed symbolically and show key              |  |  |  |  |
| representations.                               | features of the graph, by hand in simple cases and using            |  |  |  |  |
| F-IF: 7a, 7e, 9                                | technology for more complicated cases.                              |  |  |  |  |
|  | a. Graph linear and quadratic functions and show                    |  |  |  |  |
|  | intercepts, maxima, and minima.                                     |  |  |  |  |
|  | e. Graph exponential and logarithmic functions,                     |  |  |  |  |
|  | showing intercepts and end behavior, and                            |  |  |  |  |
|  | trigonometric functions, showing period, midline,                   |  |  |  |  |
|  | and amplitude.  |  |  |  |  |
|  | 9. Compare properties of two functions each represented             |  |  |  |  |
|  | in a different way (algebraically, graphically, numerically         |  |  |  |  |
|  | in tables, or by verbal descriptions). For example, given a         |  |  |  |  |

|  | aranh of one guadratic function and an algebraic   |  |  |  |
|--|--|--|--|--|
|  | graph of one quadratic function and an algebraic expression for another, say which has the larger  |  |  |  |
|  | expression for another, say which has the larger maximum.  |  |  |  |
| <b>Building Functions (F-BF)</b>   |  |  |  |  |
| Build a function that models a   | 1. Write a function that describes a relationship between  |  |  |  |
| relationship between two quantities.                                     | 1. Write a function that describes a relationship between  |  |  |  |
| F-BF: 1a, 1b, 2  | two quantities.  |  |  |  |
| 1°-D1°. 1a, 10, 2  | a. Determine an explicit expression, a recursive process, or steps for calculation from a context. |  |  |  |
|  | b. Combine standard function types using arithmetic  |  |  |  |
|  | operations. For example, build a function that   |  |  |  |
|  | models the temperature of a cooling body by  |  |  |  |
|  | adding a constant function to a decaying   |  |  |  |
|  | exponential, and relate these functions to the   |  |  |  |
|  | model.   |  |  |  |
|  | 2. Write arithmetic and geometric sequences both   |  |  |  |
|  | recursively and with an explicit formula, use them to  |  |  |  |
|  | model situations, and translate between the two forms.   |  |  |  |
| Build new functions from existing  | 3. Identify the effect on the graph of replacing $f(x)$ by $f(x)$                                  |  |  |  |
| functions.   | +k, k f(x), f(kx), and f(x + k) for specific values of k (both                                     |  |  |  |
| F-BF: 3  | positive and negative); find the value of <i>k</i> given the                                       |  |  |  |
|  | graphs. Experiment with cases and illustrate an  |  |  |  |
|  | explanation of the effects on the graph using technology.  |  |  |  |
|  | Include recognizing even and odd functions from their  |  |  |  |
|  | graphs and algebraic expressions for them.   |  |  |  |
| Linear, Quadratic and Exponential Mod                                    |  |  |  |  |
| Construct and compare linear models                                      | 2. Construct linear and exponential functions, including   |  |  |  |
| and exponential models and solve   | arithmetic and geometric sequences, given a graph, a   |  |  |  |
| problems.  | description of a relationship, or two input-output pairs   |  |  |  |
| F-LE: 2  | (including reading these from a table).  |  |  |  |
| Interpret expressions for functions in terms of the situation they model | 5. Interpret the parameters in a linear or exponential function in terms of a context.             |  |  |  |
| terms of the situation they model.<br>F-LE: 5                            | function in terms of a context.  |  |  |  |
|  |  |  |  |  |
| Wisconsin Standards for Mathematic                                       |  |  |  |  |
| Similarity, Right Triangles and Trigonor                                 |  |  |  |  |
| Prove theorems involving similarity.                                     | 5. Use congruence and similarity criteria for triangles to   |  |  |  |
| G-SRT: 5   | solve problems and to prove relationships in geometric   |  |  |  |
| Define trigenemetric   | figures.   |  |  |  |
| Define trigonometric ratios and solve                                    | 8. Use the Pythagorean Theorem to solve right triangles in   |  |  |  |
| <b>problems involving right triangles.</b><br>G-SRT: 8                   | applied problems.  |  |  |  |
|  | quations (C-CPF)   |  |  |  |
| Expressing Geometric Properties with E                                   | 5. Prove the slope criteria for parallel and perpendicular   |  |  |  |
| Use coordinates to prove simple geometric theorems algebraically.        | lines and use them to solve geometric problems (e.g., find   |  |  |  |
| G-GPE: 5, 7  | the equation of a line parallel or perpendicular to a given  |  |  |  |
| 0-01 E. J, /   | line that passes through a given point).   |  |  |  |
|  | 7. Use coordinates to compute perimeters of polygons and   |  |  |  |
|  | areas of triangles and rectangles, e.g., using the distance  |  |  |  |
|  | formula.   |  |  |  |
|  |  |  |  |  |

| Geometric Measurement and Dimension      | (G-GMD)  |  |  |  |  |
|--|--|--|--|--|--|
| Explain volume formulas and use them     | 3. Use volume formulas for cylinders, pyramids, cones,       |  |  |  |  |
| to solve problems.                       | and spheres to solve problems.                               |  |  |  |  |
| G-GMD: 3                                 |  |  |  |  |  |
| Visualize relationships between two-     | 4. Identify the shapes of two-dimensional cross-sections     |  |  |  |  |
| dimensional and three-dimensional        | of three dimensional objects, and identify three-            |  |  |  |  |
| objects.                                 | dimensional objects generated by rotations of two-           |  |  |  |  |
| G-GMD: 4                                 | dimensional objects.   |  |  |  |  |
| Wisconsin Standards for Mathematic       |  |  |  |  |  |
| Interpreting Categorical and Quantitativ |  |  |  |  |  |
| Summarize, represent, and interpret      | 1. Represent data with plots on the real number line (dot    |  |  |  |  |
| data on a single count or measurement    | plots, histograms, and box plots).                           |  |  |  |  |
| variable.                                | 2. Use statistics appropriate to the shape of the data       |  |  |  |  |
| S-ID: 1, 2, 3                            | distribution to compare center (median, mean) and spread     |  |  |  |  |
| <b>5-11</b> , 1, 2, 5                    | (interquartile range) of two or more different data sets.    |  |  |  |  |
|  | 3. Interpret differences in shape, center, and spread in the |  |  |  |  |
|  |  |  |  |  |  |
|  | context of the data sets, accounting for possible effects of |  |  |  |  |
| <b>C</b>                                 | extreme data points (outliers).                              |  |  |  |  |
| Summarize, represent, and interpret      | 5. Summarize categorical data for two categories in two-     |  |  |  |  |
| data on two categorical and              | way frequency tables. Interpret relative frequencies in the  |  |  |  |  |
| quantitative variables.                  | context of the data (including joint, marginal, and          |  |  |  |  |
| S-ID: 5, 6a, 6b, 6c                      | conditional relative frequencies). Recognize possible        |  |  |  |  |
|  | associations and trends in the data.                         |  |  |  |  |
|  | 6. Represent data on two quantitative variables on a         |  |  |  |  |
|  | scatter plot, and describe how the variables are related.    |  |  |  |  |
|  | a. Fit a function to the data; use functions fitted to       |  |  |  |  |
|  | data to solve problems in the context of the data.           |  |  |  |  |
|  | Use given functions or choose a function                     |  |  |  |  |
|  | suggested by the context. Emphasize linear and               |  |  |  |  |
|  | exponential models.  |  |  |  |  |
|  | b. Informally assess the fit of a function by plotting       |  |  |  |  |
|  | and analyzing residuals.                                     |  |  |  |  |
|  | c. Fit a linear function for a scatter plot that suggests    |  |  |  |  |
|  | a linear association.  |  |  |  |  |
| Interpret linear models.                 | 7. Interpret the slope (rate of change) and the intercept    |  |  |  |  |
| S-ID: 7                                  | (constant term) of a linear model in the context of the      |  |  |  |  |
|  | data.  |  |  |  |  |
| Making Inferences and Justifying Conclu  | usions (S-IC)  |  |  |  |  |
| Understand and evaluate random           | 1. Understand statistics as a process for making inferences  |  |  |  |  |
| processes underlying statistical         | about population parameters based on a random sample         |  |  |  |  |
| experiments.                             | from that population.  |  |  |  |  |
| S-IC: 1                                  |  |  |  |  |  |
| Make inferences and justify              | 3. Recognize the purposes of and differences among           |  |  |  |  |
| conclusions from sample surveys,         | sample surveys, experiments, and observational studies;      |  |  |  |  |
| experiments, and observational studies.  | explain how randomization relates to each.                   |  |  |  |  |
| S-IC: 3                                  |  |  |  |  |  |
| Conditional Probability and the Rules of | Probability (S-CP)   |  |  |  |  |
| Understand independence and              | 1. Describe events as subsets of a sample space (the set of  |  |  |  |  |
| conditional probability and use them to  | outcomes) using characteristics (or categories) of the       |  |  |  |  |
| interpret data.                          |  |  |  |  |  |
| ··· •                                    | 1  |  |  |  |  |

| S-CP: 1, 2 | <ul> <li>outcomes, or as unions, intersections, or complements of other events ("or," "and," "not").</li> <li>2. Understand that two events A and B are independent if the probability of A and B occurring together is the product of their probabilities, and use this characterization</li> </ul> |
|------------|--|
|            | to determine if they are independent.  |

| Key Vocabulary:              |                     |                      |                     |  |  |
|------------------------------|---------------------|----------------------|---------------------|--|--|
| Expression                   | Ratio               | Pythagorean theorem  | Similar figures     |  |  |
| Equation                     | Unit rate           | Square root          | Congruent figures   |  |  |
| Like-terms                   | Proportion          | Monomial             | Slant height        |  |  |
| Exponents                    | Scale               | Interest             | Diameter            |  |  |
| Absolute value               | Dilation            | Linear equation      | Radius              |  |  |
| Integer                      | Function            | Slope                | Volume              |  |  |
| Rational number              | Evaluate            | Slope-intercept form | Surface area        |  |  |
| Irrational number            | Percent             | Compound interest    | Cross Section       |  |  |
| Parallel lines               | Perpendicular lines | Cartesian Plane      | Scatter Plot        |  |  |
| Units of Quantity            | Linear Equations    | Linear Inequalities  | Formula             |  |  |
| <b>Exponential Equations</b> | Function Notation   | Linear Functions     | Recursive           |  |  |
| Exponential Functions        | Domain              | Range                | Arithmetic Sequence |  |  |
| Geometric Sequence           | Explicit            | Histogram            | Line of best fit    |  |  |
| Translation                  | Rotation            | Reflection           | Congruent Triangles |  |  |
| Vertex                       | Venn Diagram        | Sample Population    | Probability         |  |  |

# **Topics/Content Outline- Units and Themes:**

### Quarter 1:

- Number Sense and Operation
- Relationships with Quantities
- Reasoning with Equations

#### Quarter 2:

- Algebra Concepts
- Linear and Exponential Relationships

## Quarter 3:

- Geometry and Measurement
- Congruence, Proof, and Construction

#### **Quarter 4:**

- Connecting Algebra and Geometry Through Coordinates
- Data Analysis, Statistics and Probability

Primary Resource(s): Renaissance Learning - Accelerated Math & STAR Math assessment